

Technical Analysis Strategy Optimization using a Machine Learning Approach in Stock Market Indices

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Abstract

Within the area of stock market prediction, forecasting price values or movements is one of the most challenging issue. Because of this, the use of machine learning techniques in combination with technical analysis indicators is receiving more and more attention. In order to tackle this problem, in this paper we propose a hybrid approach to generate trading signals. To do so, our proposal consists of applying a technical indicator combined with a machine learning approach in order to produce a trading decision. The novelty of this approach lies in the simplicity and effectiveness of the hybrid rules as well as its possible extension to other technical indicators. In order to select the most suitable machine learning technique, we tested the performances of Linear Model (LM), Artificial Neural Network (ANN), Random Forests (RF) and Support Vector Regression (SVR). As technical strategies for trading, the Triple Exponential Moving Average (TEMA) and Moving Average Convergence/Divergence (MACD) were considered. We tested the resulting technique on daily trading data from three major indices: Ibex35 (IBEX), DAX and Dow Jones Industrial (DJI). Results achieved show that the addition of machine learning techniques to technical analysis strategies improves the trading signals and the competitiveness of the proposed trading rules.

Keywords: Stock market prediction, Machine learning, Technical analysis

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1. Introduction

Predicting stock prices is a growing area of interest in both academic and financial economy fields. Despite the efforts made to develop new techniques, strategies and measures, none of them have proven to be particularly effective. Stock market prediction is a challenging problem since it is affected by different factors (many of which are unknown) and the market volatility that is difficult to capture in a model. Furthermore, this kind of data is very hard to predict since it presents non-linear relationships that are non-stationary with high heteroscedasticity [40, 57, 25, 4, 9].

Such difficulties have led to the efficient-market hypothesis [45] (EMH), which states that asset prices already take into account the information based both on past and future events. According to EMH, it is not possible to predict future prices based on historical data since for such purpose it is necessary to possess privileged information. Some critics to EMH point to the psychological biases that investors exhibit under uncertainty, leading to irrational and unpredictable behaviours [32]. Nowadays there is no consensus about EMH and the debate is still ongoing.

In a more recent work, the adaptive markets hypothesis [31] (AMH) has been proposed to overcome the behavioural critics made to EMH arguing that markets are not rational, but are rather driven by fear and greed. AMH tackles the stock market from a biological perspective within an evolutionary framework in which prices evolve according to competition, adaptation, and natural selection to financial interactions. According to AMH, predictable patterns may appear over time for short periods.

Traditionally, the two most widely used approaches to analyze stock market data are fundamental and technical analysis [3]. Fundamental analysis relies on the concept of *intrinsic value*, which means that the current price is based on quantitative and qualitative information. This approach adopts the EMH in the long-term. However, in the short term it assumes that there may be some inefficiencies. Technical analysis, on the other hand, is based on historical data to find patterns and predicts the future price movements of a stock. In contrast to fundamental analysis, this approach is mainly focused on the short term [43].

In addition to technical and fundamental analysis, many researchers formulate the problem of stock price prediction as a problem of time series forecasting. Within this approach, there are basically two categories of techniques: conventional and machine learning methods. Conventional strategies

38 include, among others, statistical analysis, smoothing and regression-based
39 techniques. For example, in [26] regression-based methods have been eval-
40 uated on the top 4 stock exchanges—New York, London, NASDAQ and
41 Karachi stock exchange. They also evaluated them on the top 3 compa-
42 nies—Apple, Microsoft, and Google. The auto-regressive integrated moving
43 average (ARIMA) is used in [7] for short-term prediction of New York Stock
44 Exchange (NYSE) and Nigeria Stock Exchange (NSE), while in [56], it is
45 also used for short-term prediction of Amman Stock Exchange (ASE).

46 In recent years, there has been a growing interest in machine learning
47 based techniques. The main reason is that in contrast to conventional meth-
48 ods, these techniques are more suitable to handle complex data with non-
49 linear relationships. Within this field, artificial neural networks (ANNs) are a
50 very popular approach and have been applied in numerous works. In [35], sev-
51 eral ANN models are applied to forecast daily NASDAQ data. This method
52 has also been applied to tick data from Indian stock index in [47]. An ANN
53 with a different optimization function is proposed in [36] and is tested on
54 daily data from seven stock indices. In more recent works, Deep Learning
55 (DL) is gaining popularity. For example, [48] and [23] use a DL strategy to
56 forecast daily data from Dow 30 companies and National Stock Exchange
57 of India (NSEI) and the NYSE, respectively. Other popular techniques are
58 Support Vector Regression [22], tree-based algorithms [10], etc.

59 In this work we propose a novel hybrid trading strategy that combines
60 machine learning techniques with technical analysis indicators to generate
61 profitable trades. For such purpose, the trading rules are designed taking
62 into account the asymmetric return distribution [15] to avoid false signals and
63 achieve successful trading transactions. Results suggest that the integration
64 of the information about the predicted trend (using machine learning) to the
65 technical analysis leads to more robust signals.

66 The machine learning techniques analyzed in this paper are: Multivariate
67 Linear Regression or Linear Model (LM), Artificial Neural Network (ANN),
68 Random Forests (RF) and Support Vector Regression (SVR). As techni-
69 cal analysis strategies, the Triple Exponential Moving Average (TEMA)
70 crossover, a strategy based on the Exponential Moving Average (EMA) indi-
71 cator, and the Moving Average Convergence Divergence (MACD) are used.
72 The proposed strategy was tested on three major indices -Ibex35 (IBEX),
73 DAX and Dow Jones Industrial (DJI)- from 2011 to 2019. We can summa-
74 rize the contributions of this work as follows:

- 75 • Analyze the performance of the predictive models induced with LM,
76 ANN, RF and SVR.
- 77 • Study the return of the technical analysis-based strategies TEMA and
78 MACD.
- 79 • Propose a hybrid trading strategy that combines machine learning and
80 technical analysis.
- 81 • Develop a workflow to calculate the performance of the proposed strat-
82 egy and compare it with technical analysis-based strategies.

83 The rest of the paper is organized as follows. Section 2 introduces the
84 problem studied. Then, in Section 3, the machine learning methods, the
85 technical indicators and strategies are presented. The data used in order
86 to assess the effectiveness of our proposal is described in Section 4. The
87 experimental results are presented in Section 5, and finally, we draw the
88 main conclusions and discuss possible future developments in section 6.

89 2. Stock Market Forecasting

90 Stock market values consist of a discrete sequence of time-ordered data
91 points measured at equal time intervals. Given \mathcal{E} a set of n samples char-
92 acterized by T real values x_1, \dots, x_T , ($1 \leq i \leq T$) so that x_i represents
93 the recorded value at time i , let w be the historical window and h the
94 prediction horizon so that $w + h \leq T$. Then, the associated time series
95 forecasting problem can be formulated as the problem of predicting the val-
96 ues of x_{w+1}, \dots, x_{w+h} , given x_1, \dots, x_w ($w + h \leq T$), with the objective of
97 minimizing the error between the predicted value \hat{x}_{w+i} and the actual value
98 x_{w+i} ($1 \leq i \leq h$). A more extensive introduction to time series analysis can
99 be found in [12].

100 2.1. Related work

101 As previously mentioned, the application of machine learning techniques
102 to the stock market forecasting problem has gained popularity in recent years.
103 This is due, among others, for the suitability of such techniques to handle
104 complex relations and the advances in computer technology that allow to
105 process massive amounts of data.

106 In an early work, Yao et al. [58] investigate the performance of the au-
107 toregressive integrated moving average (ARIMA) and the ANNs techniques
108 for forecasting the Kuala Lumpur Composite Index (KLCI). The indicators
109 moving average (MA), momentum (M), Relative Strength Index (RSI), and
110 stochastics %K and moving average of stochastics %D (KD) are used as
111 the inputs of the ANN. The trading rules, which are based on such predic-
112 tions, are tested on daily data collected from January 3, 1984 to October
113 16, 1991. In another work, Pérez-Rodríguez et al. [42] propose a combi-
114 nation of the filter techniques [5] trading strategy with smooth transition
115 autoregression (STAR) models and ANNs. The study is conducted on daily
116 data from the Spanish IBEX stock index return gathered over the period
117 going from December 30, 1989 to February 10, 2000. In [13] Chang et al.,
118 the authors propose a combination of ANN with Piecewise Linear Repre-
119 sentation (PLR) model to make trading decisions. This strategy receives
120 as input, a set of technical indicators -MA, Bias (BIAS), RSI, KD, MACD,
121 Williams %R (WR), Transaction Volume (TV) and Differences of technical
122 indexes (Δ)-, which are processed to produce trading signals. This proposal
123 is tested on nine different stocks -AU Optronics (AUO), Epistar Corporation
124 (EPISTAR), GP, Silicon Integrated System Corporation (SiS), SENAIO In-
125 ternational Corporation (SENAO), D-Link Corporation (D-LINK), Foxlink
126 Corporation (FOXLINK), Compal Corporation (COMPAL) and UMC Cor-
127 poration (UMC)- collected from January 2, 2004 to April 12, 2006.

128 Teixeira and Oliveira [53] combine technical analysis and k nearest neigh-
129 bor (kNN) classifier for automatic trading. The indicators MA, RSI, KD,
130 and Bolinger Bands (BB) are calculated and used as input of the kNN model.
131 Authors compare the results of the proposed trading rule with a buy-and-
132 hold strategy on fifteen stocks from São Paulo Stock Exchange. The data
133 collected covered a period going from April 1, 1990 to March 9, 2009. In an-
134 other work R. Dash and K. Dash [18] propose a decision support system that
135 integrates technical analysis and a computational efficient functional link
136 ANNs (CEFLANNs). First, the proposed workflow learns the trends from
137 data computed from the the technical indicators MA, MACD, KD, RSI and
138 WR. This information is then applied to the trading rules. The same work-
139 flow is compared using the machine learning techniques Naive Bayes, Support
140 Vector Machine (SVM), kNN and Decision Tree (DT). In this work five years
141 of historical stock index price values from BSE SENSEX and S&P500 is used.
142 The data was collected in the period comprised between January 2010 and
143 December 2014.

144 Sang and Di Pierro [46] propose the use of an ANN to improve tech-
145 nical analysis trading strategies. For each strategy considered -Simple MA
146 (SMA), RSI and MACD-, an ANN model is induced in order to determine
147 whether the strategy will produce a profit or a loss. The data used con-
148 sisted of nine indexes representing entire sectors under S&P500 recorded in
149 the period 2014-2015. Deep Learning has also been combined with stock
150 technical indicators in [1] by Agrawal et al. First, new input features are
151 created from the RSI, MA, KD, WR, Exponential MA (EMA) and MACD
152 indicators. Then, the price trend is estimated using DL and such prediction
153 is incorporated in the trading rule. The performance of DL is compared with
154 SVM and Linear Regression (LR) on data from 3 banks listed in the National
155 Stock Exchange of India. The data encompassed the trading days of 2 years:
156 from November 16, 2016 to November 15, 2018.

157 In a recent work Aguirre et al. [2] propose to hybridize MACD with a Ge-
158 netic Algorithm (GA) to optimize the parameters that generate the buy-sell
159 signals. The proposal is compared with MACD and Buy & Hold strategies on
160 data from NASDAQ stock index over a seven-year period: from January 1,
161 2013 to December 31, 2019. The article from Chen et al. [16] introduce a novel
162 hybrid DL model that integrates Attention Mechanism (AM), Multi-Layer
163 Perceptron (MLP), and Bidirectional Long-Short Term Memory (BiLSTM)
164 ANN. First, the strategy creates a knowledge base comprised of 31 features
165 obtained from historical prices of stocks, technical indicators and natural
166 resources prices and historical data of the Google index. Then, the dimen-
167 sionality is reduced by applying Principal Components Analysis (PCA). After
168 this phase, the hybrid DL approach is applied to forecast the closing price.
169 The technical indicators used in this work are MA, EMA, RSI, Chande Mo-
170 mentum Oscillator (CMO), Commodity Channel Index (CCI), MACD, Per-
171 centage Price Oscillator (PPO), Triangular Moving Average (TMA), KD,
172 Chaikin A/D Oscillator (CAD), BB and WR. The model is compared with
173 Support Vector Regression (SVR), LSTM, Convolutional Neural Network
174 (CNN), MLP and MLP+BiLSTM. The robustness of the proposed model
175 was proven through testing on the stock indexes S&P 500, Dow Jones (DJ),
176 NASDAQ, and Russell 2000 (Russell2000).

177 New hybrid models that integrate sentiment analysis data are also becom-
178 ing popular in recent works (see [44, 50, 28]). Despite the potential advan-
179 tage of incorporating the the market sentiment, it also presents challenging
180 difficulties such as misspelling, shortcuts and information duplication in text
181 data. Furthermore that may led to low efficiency [52]. Ensemble approaches

182 have also obtained good results when applied to the stock market prediction
 183 problem. Examples of such strategies are, for instance, [30, 39, 38, 20, 60, 39].

184 We refer the reader to [51] for a further description of additional works
 185 using machine learning strategies. A summary of the hybrid models described
 186 in this section is shown in Table 1. The first column indicates the year of
 187 the publication followed by the technical indicators considered in the work.
 188 Then, the strategy used are listed followed by the tasks addressed: F for
 189 forecasting, C for classification and T for trading signals. Next, the stock
 190 data source and the period of time collected are shown, and, finally, the
 191 relative reference is reported.

Table 1: Summary of the related works described. In the Tasks column, F refers to Forecasting, C to classification and T to trading.

Year	Indicators	Methods	Tasks	Stocks	Period	Ref.
1999	MA, M, RSI, KD	ARIMA, ANN	F, T	KLCI	03/01/1984-16/10/1991	[58]
2005	–	STAR, ANN	F, T	IBEX35	30/12/1989-10/02/2000	[42]
2009	MA, BIAS, RSI, KD, MACD, WR, TV, Δ	PLR, ANN	F, T	AUO, EPISTAR, GP, SiS, SENAO, D-LINK, FOXLINK, COMPAL, UMC	02/01/2004-12/04/2006	[13]
2010	MA, RSI, KD, BB	kNN	C, T	BM&FBovespa	01/04/1998-09/03/2009	[53]
2016	MA, MACD, KD, RSI, WR	ANN, SVM, DT	NB, C, T, kNN	BSE SENSEX, S&P500	01/01/2010-01/12/2014	[18]
2019	SMA, MACD	RSI, ANN	F, T	S&P500	01/01/2014-31/12/2015	[46]
	RSI, MA, KD, WD, EMA, MACD	DL, SVM, LR	C, T	NSEI	16/11/2016-15/11/2018	[1]
2020	MACD	GA	F, T	NASDAQ	01/01/2013-31/12/2019	[2]
	SMA, RSI, MACD, TMA, KD, BB, WR	EMA, CCI, PPO, CAD, MLP+BiLSTM	DL, SVR, F, LSTM, CNN, MLP	S&P500, NASDAQ, sell2000, DJ	NAS- 2/11/2008-12/07/2019 Rus-	[16]

192 2.2. Methods

193 In this section, we will briefly describe the methods used to produce
 194 the predictions of the experiments performed in this work. As mentioned
 195 before, in this paper we use four learning strategies that are independently
 196 trained, named Linear Model, Artificial Neural Networks, Random Forest
 197 and Support Vector Regression. These methods were selected since they have

198 proven their good performance in the field. Due to this, they are widely-used
199 in literature for regression tasks in stock market prediction, e.g., [17, 49, 59,
200 41].

201 **Linear Model (LM)** [37], also called linear regression, is a statistical ap-
202 proach that is typically used to model the relationship between two variables
203 and also for time series forecasting. The main idea behind this approach
204 is to find the relationship between two variables using a linear equation,
205 $Y = a + bX$, for representing the association between the independent vari-
206 able (X) and the dependent one (Y), i.e., the variable to be predicted. This
207 approach can also use multiple independent variables to determine the final
208 value of the dependent one, which is called multiple linear regression and
209 it is represented by the equation $Y = a + b_1X_1 + \dots + b_nX_n + \epsilon$, where
210 ϵ is the residual (difference between the predicted and the observed value)
211 and $X_i, 1 \leq i \leq n$ are the n explanatory variables. In this work, we model
212 different dependent variables from the same input dataset so, we selected the
213 multi-output regression. Multi-output regression, also known in the litera-
214 ture as multi-target, aims to simultaneously predict multiple output/target
215 variables.

216 In this paper, we have used the implementation provided by R caret
217 package [27].

218 **Artificial Neural Networks (ANN)** [21], are computational models
219 for classification and regression. They are inspired by the human brain neural
220 networks. An ANN is formed by a set of connected nodes, called (*neurons*),
221 that are interconnected with each other simulating the connections of the
222 brain. The information is transmitted from neuron to neuron and the learn-
223 ing is achieved through training data. ANNs are composed by different layers:
224 an input layer, one or more hidden layers, and an output layer. Connections
225 among nodes of different layers are weighted. Thus, the information is car-
226 ried from one layer to another using an *activation function* that accounts
227 for the non-linearity in the data. This process, which is called feed-forward
228 propagation, defines how the data are fed into the next layers. The model
229 learns by minimizing a *loss* function that calculates the data prediction error
230 by adjusting the weight of the connections. The final prediction is computed
231 in the output layer, where a transformation function is used in the final step.
232 The number of neurons in the input layer varies and depends on the dimen-
233 sionality of the input data, while in the output layer this number depends
234 on the expected output. In the case of regression tasks, a single neuron that
235 offers a final numerical value is used.

236 In this work we use a feed-forward ANN that consists of an input layer,
237 one hidden layer, and an output layer. No feedback or lateral connections
238 were used. The algorithm developed in the R package `nnet` [55] was used.

239 **Random Forests (RF)** is an ensemble method that may be applied for
240 both classification and regression tasks. The prediction model induced by
241 RF consists of a set of decision trees, and the final prediction is computed
242 considering the predictions of each tree, e.g., with a majority vote in the
243 case of classification. For regression tasks, the final prediction consists of the
244 average of the trees' predictions. The trees induced are independently trained
245 with a bootstrap sample of the training data (*Bagging* ensemble method)
246 selecting a random number of features. RF was first proposed by Ho [24]
247 and improved by Breiman [11], combining the random sub-set method with
248 its bagging method. RFs offer a way of averaging multiple trees with a low
249 variance for predictions, since each tree is formed with a random subset of
250 data and features. In this paper we used the implementation provided by
251 the R package [29], which is based on the Breiman's algorithm. `lausugum`

252 **Support Vector Regression (SVR)** [8], is a variant of support vector
253 machines (SVM), adapted for being used for regression and forecasting tasks.
254 SVR applies the same criteria as SVM for classification. SVR is characterized
255 by the use of kernels, sparse solution, and VC control of the margin and the
256 number of support vectors. In spite of their similarities, SVR presents some
257 minor differences with SVM.

258 Since the output is a real number, it is difficult to predict an exact value,
259 since there are infinite possibilities. However, the main idea is the same:
260 minimize the error, finding the hyper plane that maximizes the margin by
261 taking into account that part of the error is tolerated.

262 In this work, the implementation provided by the R `caret` package was
263 used [27].

264 2.3. Performance metrics

265 In this section, we introduce the metrics used to assess the quality of the
266 learning methods used in this paper. In particular, we use four measures that
267 are commonly used in regression: the mean absolute error (MAE), the root
268 mean squared error (RMSE), the mean absolute percentage error (MAPE)
269 and the symmetric mean absolute percentage error (sMAPE).

270 Given the sample size n , the actual observation y_t at time t , $1 \leq t \leq T$,
271 and the prediction \bar{y}_t , the metrics are defined as follows:

- 272 • **Mean absolute error (MAE)** measures the average over a sample of
273 the absolute differences between the predicted and actual observation.
274 It is defined by the following formula:

$$MAE = \frac{1}{n} \sum_{t=1}^n |y_t - \bar{y}_t|$$

275 The MAE is a linear score. This means that all the single differences
276 are considered equally in the average. It follows that larger errors will
277 contribute linearly to the total error. This represents the main draw-
278 back of this measure, as outliers may affect its meaning. An advantage
279 of using MAE is that it is an intuitive and easy to interpret measure.

- 280 • **Root mean squared error (RMSE)** also measures the average mag-
281 nitude of the errors, and it is defined as:

$$\sqrt{\frac{1}{n} \sum_{t=1}^n (y_t - \bar{y}_t)^2}$$

282 Notices that this measure is a quadratic scoring rule. It follows that
283 it measures the average magnitude of the error. In this sense outliers
284 have a greater impact on this measure.

- 285 • **Mean absolute percentage error (MAPE)** measures how accurate,
286 as a percentage, a forecasting system is. It is calculated as follows:

$$MAPE = \frac{1}{n} \sum_{t=1}^n \left| \frac{y_t - \hat{y}_t}{y_t} \right|$$

287 We can state that MAPE is basically the percentage equivalent of MAE.
288 MAE is the average magnitude of error produced by a model, while
289 MAPE represent how far, on average, the predictions are from the real
290 values. As for MAE, MAPE is not affected too much by the presence
291 of outliers, as it is a linear function. MAPE have a problem that is the
292 denominator is zero, then its value would be undefined.

- 293 • **Symmetric mean absolute percentage error [33] (sMAPE)** is a
294 modified version of MAPE to fix the issues of being infinite or undefined

295 due to zeros in the denominator [14], and is defined in the following
296 way:

$$sMAPE = \frac{1}{n} \sum_{t=1}^n \frac{2|y_t - \bar{y}_t|}{|y_t + \bar{y}_t|}$$

297 As already stated, sMAPE is a modified MAPE in which the divisor is
298 half of the sum of the actual and predicted values.

299 In following we report the values of MAPE and sMAPE multiplied by 10^3 ,
300 in order to avoid presenting extremely small values.

301 3. Stock Market Strategies

302 In this section, we first introduce the technical analysis indicators used
303 in this paper, namely the Exponential Moving Average, the Moving Average
304 Convergences/Divergences and the Triple Exponential Moving Average
305 crossover strategy. We also briefly describe the trading strategies associated
306 to them. After that, we continue by describing the strategy proposed in this
307 paper.

308 3.1. Technical Indicators

309 In our proposal, we use two commonly used indicators in trading strat-
310 egy, i.e., the Exponential Moving Average and the Moving Average Conver-
311 gence/Divergence indicators.

312 **Exponential Moving Average (EMA).** This is one of the most popular
313 technical indicators. EMA is used to gauge the trend of a financial asset. To
314 this aim, EMA smooths the price by filtering out the noise from random price
315 fluctuations by averaging the price over a given period of time m . EMA is
316 based on past prices and, so, it is a lagging indicator. This means that EMA
317 cannot predict new trends, but it can confirm the direction of the trend.

318 EMA assigns more weight to recent prices, and is defined as in the fol-
319 lowing formula:

$$EMA_t^m(S_t) = \begin{cases} S_1 & \text{if } t = 1, \\ \alpha \cdot S_t + (1 - \alpha) \cdot EMA_{t-1}^m & \text{if } t > 1. \end{cases}$$

320 In the above formula, S_t refers to the current price, m to the number of
321 observations and α is a smoothing factor, $0 \leq \alpha \leq 1$, that is calculated as
322 $\alpha = \frac{2}{m+1}$.

323 **Moving Average Convergence/Divergence (MACD)**. This indicator
 324 was first proposed by Gerald Appel in [6] and used to identify the trend
 325 direction and duration by calculating the relationship between two EMAs.
 326 MACD consists of two series: the MACD line ($MACD_t$) and the MACD
 327 signal series ($Signal_t$). The MACD line is obtained as the difference between
 328 the faster and the slower EMAs. The signal is the Moving Average (MA) of
 329 the MACD series. Given the time periods m , n and p so that $m < n$, then

$$\begin{aligned} MACD_t &= EMA_t^m(S_t) - EMA_t^n(S_t), \\ Signal_t &= EMA_t^p(MACD_t). \end{aligned}$$

330 3.2. Technical Analysis Strategies

331 As trading strategies, two simple strategies based on MACD and EMA
 332 indicators are selected. The description of each strategy is given below.

333 **MACD strategy**. A very common strategy based on the MACD indicator
 334 is the following:

$$Strategy_{t+1} = \begin{cases} Buy & \text{if } MACD_t > Signal_t, \\ Sell & \text{if } MACD_t < Signal_t. \end{cases}$$

335 Therefore, a potential buy signal is generated when $MACD_t$ crosses above
 336 the $Signal_t$ line and, similarly, we have a potential sell signal in the opposite
 337 scenario.

338 **Triple Exponential Moving Average (TEMA) crossover strategy**.
 339 This strategy is used to identify trends in the market and to deal with false
 340 market signals. It is based on three EMAs, for short, mid and long term
 341 periods, respectively. The EMA for short period (fast EMA) is the first one
 342 to detect a possible shift in the trend that is confirmed once it crosses both
 343 the medium and the slow EMAs. So, giving three periods of time m , n and
 344 p so that $m < n < p$, the strategy is defined as follows:

$$Strategy_{t+1} = \begin{cases} Buy & \text{if } EMA_t^m > EMA_t^n \text{ and } EMA_t^m > EMA_t^p, \\ Sell & \text{if } EMA_t^m < EMA_t^n \text{ and } EMA_t^m < EMA_t^p. \end{cases}$$

345 Therefore, the buy signal is generated once the fast MA crosses above the
 346 medium and slow MAs, while the sell signal is produced in the other case.

347 *3.3. Hybridization of Machine Learning with Technical Analysis*

348 The proposed strategy aim at improving the technical analysis trading
349 signals by incorporating the machine learning techniques in the trading rules.
350 The general scheme of the proposal is presented in Figure 1. First, stock
351 data is collected from the server. The data is then split into training and
352 test sets. The training data is used to optimize the predictive models and the
353 technical analysis based strategies. The so obtained hybrid schema is then
354 built and its performance is assessed on the test dataset. Finally, the results
355 are analyzed to establish the quality of the hybrid strategy. The main steps
356 of this workflow are:

- 357 (a) Build the optimal learning model.
- 358 (b) Optimize the technical analysis strategies.
- 359 (c) Backtest the hybrid technical analysis strategy

360 In the following we describe each step.

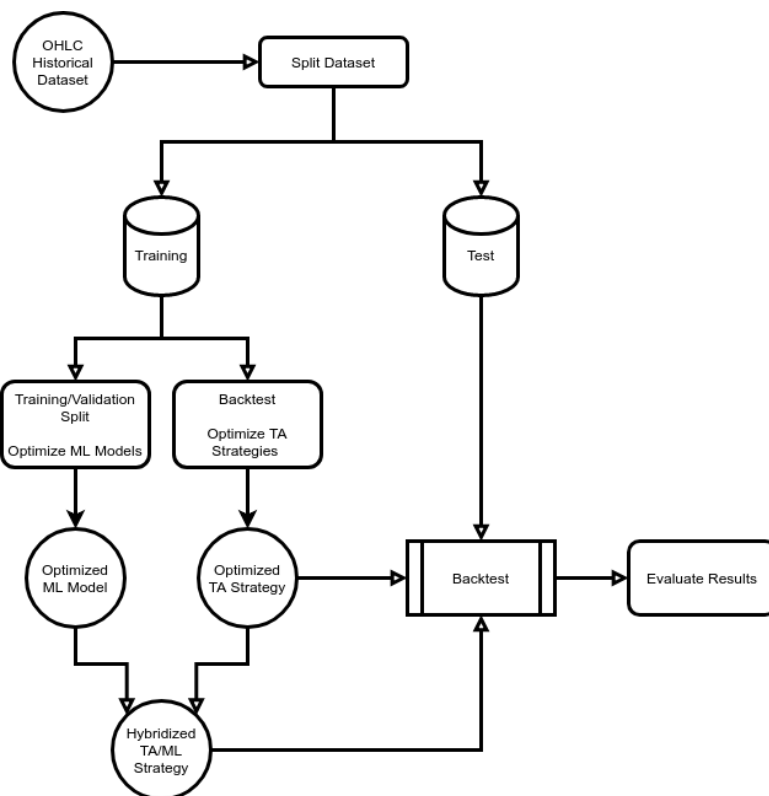


Figure 1: General scheme for backtesting the proposed trading strategy.

361 **(a) Build the optimal learning model.** The time series is pre-processed
 362 as in Divina et al. [19] using a strategy often referred to as Walk Forward
 363 Validation. In a nutshell, this strategy requires to set the number of his-
 364 torical observations w and the size of the prediction horizon h . Given the
 365 training time series observations and the values of w and h , the training su-
 366 pervised learning data is created by considering a sliding window of size $w +$
 367 h . The first instance consists of the first $w + h$ observations. For the next
 368 instance, such a window slides forward one value from x_2 to x_{w+h+1} and so
 369 on. Then, the training data is divided into training and validation datasets.
 370 This process is graphically described in Figure 2.

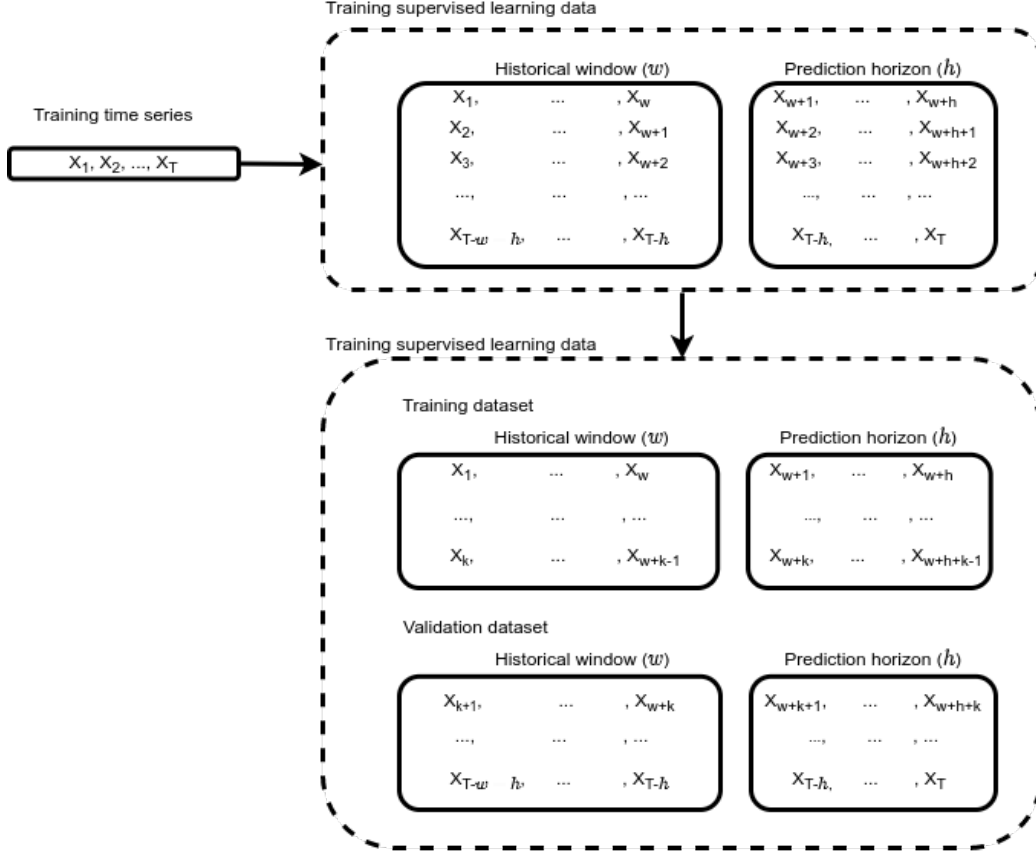


Figure 2: First, the training time series is converted to a supervised learning problem. Next, the data is split into training and validations datasets. w refers to the amount of the historical data used, while h determines the prediction horizon.

371 Before building the final predictive model, a hyperparameter tuning phase
 372 is carried out. For each combination of hyperparameters, the model is built
 373 on the training dataset and tested on the validation dataset. As a final step,
 374 the model is induced on the full training data using the optimal hyperpa-
 375 rameters found.

376 **(b) Optimize the technical analysis strategies.** In this step, the train-
 377 ing data is used for backtesting the technical analysis strategies. For this
 378 purpose, a grid search is applied on the entire training data. The parameters
 379 with the best performance will be selected for the hybridization.

380 **(c) Backtest the hybrid technical analysis strategy.** In this last step,
 381 the hybrid strategy is backtested on the test dataset. The proposed trading
 382 rules is applied and the performance evaluated.

383 3.4. Proposed trading rule

384 MACD and EMA, which belong to the family of lagged indicators, are
 385 measurable factors that trail behind the current market price. Although
 386 they are used to create trading signals, actually they are useful to confirm
 387 the strength of a long-term trend since they look retrospectively at past
 388 data [34]. Furthermore, this kind of indicators may generate false signals
 389 due to many factors such as short-term market fluctuations. Therefore, the
 390 integration of predicted price may lead to a decrease in the number of false
 391 signals.

392 The proposed rule uses the predictive model to generate trading signals.
 393 For a given day t , Buy_t and $Sell_t$ refer to the buy and sell signals given only
 394 by the technical analysis strategies. The learning model provides information
 395 about the evolution of the price. In order to decide about to enter in the
 396 market, it is useful to know the trend on the stock values. For this purpose,
 397 although larger values of h allow us to estimate the price farther in the future,
 398 the prediction error increases with h . So, in order to balance both issues, a
 399 prediction horizon of just over a month was set in this study.

400 In this context, to estimate the trend of the market, the strategy compares
 401 the price x_t at day t with the predicted value \hat{x}_{t+h} at day $t+h$. The tendency
 402 is considered as an uptrend (UT_{t+h}) if $\hat{x}_{t+h} > x_t$ and a downtrend (DT_{t+h}) if
 403 $\hat{x}_{t+h} < x_t$.

404 It is a well-known fact that the very largest movements in the market
 405 usually correspond to decrements rather than to increments [15]. This fact
 406 may favour the number of false sell signals. Therefore in our proposal the buy
 407 signal at day $t+1$ is generated if it is confirmed by the technical indicator
 408 at day t or by the estimated trend. On the other hand, the sell signal is
 409 generated if the technical indicator and the trend identify a down market
 410 movement. So, let D_{t+1} be the trading decision at day $t+1$, the trading rule
 411 is defined as follows:

$$D_{t+1} = \begin{cases} \text{Buy if } & Buy_t \text{ or } UT_{t+h} \\ \text{Sell if } & Sell_t \text{ and } DT_{t+h} \end{cases}$$

412 The use of a predictive model improves the estimation of the price trend in

413 a near future. So, despite the fact that its inclusion increases the complexity
414 of the strategy, it provides valuable and relevant information that can yield
415 better trading signals.

416 3.5. Metrics

417 The metrics used to evaluate the performance of the trading strategies
418 associated are:

- 419 • **Profit factor (PF)**. Relation between Profits and Losses:

$$PF = \left| \frac{\text{Profits}}{\text{Losses}} \right|$$

420 It follows that if $PF < 1$, then $\text{Losses} > \text{Profits}$.

- 421 • **Number of trades (#T)**. The number of trades done. A trade is
422 composed of a buy and a sell order.
- 423 • **Maximum drawdown (D_{max})**. The Worst decline-from-peak ob-
424 served in the test period.
- 425 • **Net Profit (NP)**. Sum of Profits and Losses:

$$NP = \text{Profits} - \text{Losses}$$

- 426 • **Average profit per trade (\bar{T})**. This metric is calculated by dividing
427 the net profit by the number of trades:

$$\bar{T} = \frac{NP}{\#T}$$

- 428 • **Percent profitable (PP)**. This metric is also known as the probability
429 of winning and is calculated by dividing the number of winning trades
430 by the total number of trades:

$$PP = \frac{\#T_W}{\#T}$$

431 4. Data

432 In this work we focus on daily stock exchange rates from three major in-
433 dices: IBEX, DAX and DJI. The IBEX is the major stock exchange of Spain.
434 It comprehends the 35 most liquid Spanish stocks traded in the Madrid Stock
435 Exchange General Index. The DAX is the German stock index which mea-
436 sures the performance of the 30 largest companies according to order book
437 volume and market capitalization. Finally, DJI is the stock exchange of in-
438 dustrial companies of the United States. It measures the stock performance
439 of 30 large companies.

440 Data was collected from IG Group and covers a period going from January
441 1, 2011 to December 31, 2019. Each observation is described by five features.
442 In particular, the features used are the date, the opening price, the closing
443 price, the highest price and the lowest price. A summary of the data is shown
444 in Table 2, where for each index, the starting and end days is given followed
445 by the total number of observations.

Table 2: Summary of the indices data.

Symbol	Start	End	#Observations
IBEX	2011-01-02	2019-12-31	2800
DAX	2011-01-02	2019-12-31	2799
DJI	2011-01-03	2019-12-31	2713

446 5. Experiments

447 This section describes the experiments conducted to assess the quality of
448 the proposed strategy. Such experiments can be summarized as follows:

- 449 (a) in Section 5.1, a comparison of the performances of the machine learn-
450 ing techniques used is proposed.
- 451 (b) the optimization of the technical analysis strategies TEMA and MACD
452 is reported in Section 5.2.
- 453 (c) section 5.3 presents the backtesting performed with the proposed hy-
454 brid trading strategy and its results compared with TEMA and MACD
455 strategies.

456 In the experiments, each buy or sell order is executed the next day after
 457 a signal is generated. The order size is the same for all entrances. In order
 458 to fix the spread values, we have considered the values set by IG Group at
 459 regular trading hours in Europe. Thus, the spread of each trade is fixed to
 460 5, 2, and 2.4 for *IBEX*, *DAX* and *DJI* respectively.

461 *5.1. Analysis of the learning schemes*

462 In this section the machine learning techniques used in this paper, i.e.,
 463 LM, ANN, RF and SVR, are compared. The hyperparameter optimization
 464 for each learning scheme was performed using a grid search. To facilitate
 465 the readability of this section, only the parameters values found for each
 466 technique are shown in Table 3. Tables reporting the average results over
 467 the prediction horizon h , are presented in Section Appendix A. In order to
 468 select the optimal parameters, the best values, averaged over w and h , found
 469 for each technique were selected. These values are shown in Table 4.

Table 3: Optimal parameters for each learning scheme.

A	Parameter		Description
LM	-		-
ANN	#It.	= 500	Maximum number of iterations
	Size	= 1	Number of units in the hidden layer
	Decay	= 0	The weight decay
RF	#Trees	= 100	Number of trees to grow
	#Nodes	= 100	Maximum number of terminal nodes
SVR	kernel	= linear	Kernel type
	ε	= 0.1	Insensitive-loss function
	tolerance	= 0.001	Tolerance for stopping criterion

470 Table 4 reports the performance of each method on the test set. For each
 471 method and stock market we report the average over all historical windows w
 472 and prediction horizons h of the measures MAE, RMSE, sMAPE and MAPE,
 473 together with the standard deviation. As it can be noticed, the best results
 474 are achieved by LM and ANN, followed closely by SVR. RF models are, by
 475 far, the worse ones. It can be seen that the more the stock values vary, the
 476 higher the error is.

Table 4: Performance of each learning algorithm averaged over the historical window w and the prediction horizon h . For each metric and algorithm, the average results together with its standard deviation is reported.

w	Metric	LM	ANN	RF	SVR
IBEX	MAE	175.76 ± 2.88	180.40 ± 2.59	204.08 ± 9.84	177.35 ± 5.07
	RMSE	226.20 ± 2.64	231.60 ± 2.79	259.08 ± 12.24	228.33 ± 4.61
	sMAPE ¹	18.45 ± 0.35	18.92 ± 0.32	21.50 ± 1.06	18.58 ± 0.58
	MAPE ¹	18.41 ± 0.34	18.86 ± 0.30	21.43 ± 1.00	18.51 ± 0.56
DAX	MAE	257.97 ± 3.70	260.00 ± 4.92	625.47 ± 144.60	259.11 ± 4.98
	RMSE	326.63 ± 6.05	331.99 ± 7.81	749.97 ± 148.81	329.75 ± 8.09
	sMAPE ¹	21.15 ± 0.31	21.28 ± 0.40	51.30 ± 12.13	21.22 ± 0.41
	MAPE ¹	21.10 ± 0.29	21.15 ± 0.37	53.19 ± 12.95	21.11 ± 0.37
DJI	MAE	487.69 ± 10.09	476.52 ± 9.65	4614.25 ± 63.61	493.45 ± 12.14
	RMSE	638.27 ± 11.25	635.91 ± 11.70	4900.81 ± 93.46	643.72 ± 14.44
	sMAPE ¹	19.46 ± 0.39	18.99 ± 0.36	200.62 ± 3.74	19.69 ± 0.46
	MAPE ¹	19.44 ± 0.40	18.92 ± 0.35	226.00 ± 5.03	19.66 ± 0.46

¹ × 10⁻³.

477 *5.2. Optimize technical analysis strategies*

478 Throughout this section, the performance of MACD and TEMA strategies
479 will be analyzed. The optimal combination of parameter values are sought
480 for with a grid search on data ranged from January 1, 2011 to December 31,
481 2018.

482 Table 5 presents the range of values considered for each strategy. For
483 TEMA and MACD, the combination of parameter values were restricted to
484 follow the rules *Fast < Medium < Slow* and *Fast < Slow*, respectively.

Table 5: Parameter ranges considered for TEMA and MACD trading strategies to find the optimal combination.

A	Parameter	Description
TEMA	Fast	[1, 25]
	Medium	[5, 50]
	Slow	[10, 75]
MACD	Fast	[1, 25]
	Slow	[5, 75]
	Signal	[5, 25]

485 The top 5 best combinations of parameters are presented in Table 6.
486 We can notice that the behaviour of both strategies differ when applied
487 to the indices. For both trading strategies, the best results are achieved
488 with DJI index, followed by DAX and IBEX. MACD outperforms TEMA
489 on IBEX and DAX while it underperforms on DJI data. On IBEX, TEMA
490 is a non profitable strategy since it reaches values below 1. Despite MACD
491 is profitable, the values on test data may be unprofitable due to taxes and,
492 furthermore, the expected return does not compensate the risk taken. On
493 DAX, only in the case of MACD the return expected is interesting enough.
494 However, if we take into account that the performance of the strategies are
495 lower on new data, we can discard both strategies for a real trading. Finally,
496 on DJI, the achieved results can be considered competitive, especially for the
497 case of TEMA, which reaches PF values close to 4. To sum things up, we
498 can state that only on DJI the TEMA and MACD strategies are competitive
499 and are expected to be profitable according to the profit factor.

Table 6: The performance of the top 5 combination of parameters for TEMA and MACD.

Strategy	Index					
	IBEX		DAX		DJI	
	Parameters	PF	Parameters	PF	Parameters	PF
TEMA	(2, 6, 10)	0.943	(14, 30, 74)	1.364	(18, 34, 54)	3.900
	(2, 5, 10)	0.940	(14, 31, 74)	1.364	(18, 35, 54)	3.900
	(2, 7, 10)	0.918	(3, 25, 35)	1.341	(18, 36, 54)	3.900
	(2, 9, 10)	0.916	(19, 26, 64)	1.330	(21, 22, 50)	3.845
	(1, 8, 12)	0.913	(19, 27, 64)	1.330	(21, 23, 50)	3.845
MACD	(9, 19, 6)	1.056	(3, 11, 6)	1.629	(3, 28, 9)	2.003
	(5, 12, 17)	1.047	(5, 8, 5)	1.629	(2, 34, 11)	1.998
	(6, 19, 9)	1.043	(3, 7, 11)	1.621	(2, 25, 13)	1.988
	(5, 13, 16)	1.038	(3, 6, 11)	1.619	(2, 27, 11)	1.987
	(2, 30, 13)	1.037	(4, 5, 11)	1.619	(2, 29, 12)	1.985

500 5.3. Backtest the trading strategies

501 Finally, the trading strategies are backtested on 2019 data using the op-
502 timal parameter values of TEMA and MACD strategies. According to the
503 results achieved in Section 5.1, LM and ANN are the best strategies. Follow-
504 ing Occam’s razor principle, we selected LM. In order to set the size of the
505 historical windows w Tables A.8, A.9, and A.10 are taken into account. For
506 each stock, the w with which LM achieved the lowest error was selected. The

507 LM models were built setting w to 72, 12 and 96 for IBEX, DAX and DJI,
508 respectively. To generate the trading signal, the model considered $h = 24$
509 since it allows to better capture the trend of the price.

510 The results on test data are shown in Table 7, where, for each strategy
511 and index, we report the best combination of parameters found on the train-
512 ing set, the total number of trades ($\#T$), the profit factor (PF), the net
513 profit (NP), the average profit per trade (\bar{T}) and the maximum drawdown
514 (D_{max}). Finally, in the last column, the percent profitable (PP) is shown.
515 The proposed strategies are denoted as hybrid TEMA (hTEMA) and hybrid
516 MACD (hMACD). The values associated to the metrics NT, \bar{T} and D_{max} are
517 given in points.

518 As it can be seen, the hybridization yield an improvement of the profit of
519 each strategy for all indices as well as a reduction of the number of trades. As
520 previously seen, on IBEX, the hybridization allow to have profitable strate-
521 gies. On DAX and DJI, despite having strategies positive NT, hTEMA and
522 hMACD improved the profitability. Furthermore, the proposed strategy does
523 not present any lost trade.

524 It can also be noted that only in the case of IBEX, the drawdown exceeds
525 the net profit. hMACD outperforms hTEMA on DAX and DJI while it
526 underperforms on IBEX. If, for example we have a portfolio of \$10000, and
527 each point is supposed to be equivalent to \$1, then the total profit on IBEX
528 would be of \$866.1 and \$300.5 for hTEMA and hMACD respectively. For
529 DAX, the return would be of \$2211.8 and \$1817.1 and, finally, for DJI, of
530 \$2678 and \$2738.9.

Table 7: Comparison of the performance of the trading strategies with and without hybridization using the optimal parameter values found for TEMA and MACD indicators.

Index	Strategy	Parameters	#T	PF	NT	\bar{T}	D_{max}	PP
IBEX	TEMA	(2, 6, 10)	19	0.705	-403.6	-21.2	-1052.5	42.11
	hTEMA		2	∞	866.1	433.1	-1033.1	100.00
	MACD	(9, 19, 6)	19	0.518	-807.6	-42.5	-1627.0	31.58
	hMACD		2	∞	300.5	150.3	-1228.0	100.00
DAX	TEMA	(14, 30, 74)	2	∞	1350.0	675.0	-1072.0	100.00
	hTEMA		1	∞	2211.8	2211.8	-1260.6	100.00
	MACD	(3, 11, 16)	33	1.117	303.9	9.2	-1083.5	36.36
	hMACD		3	32.991	1817.1	605.7	-1260.6	66.67
DJI	TEMA	(18, 34, 54)	4	1.478	470.5	117.6	-2402.3	25.00
	hTEMA		1	∞	2678.0	2678.0	-2151.5	100.00
	MACD	(3,28, 9)	20	1.307	1046.1	52.3	-2108.2	40.00
	hMACD		2	∞	2738.9	1369.5	-2151.5	100.00

531 The trades with TEMA and hTEMA on IBEX, DAX and DJI are shown
532 in Figure B.3 while for MACD and hMACD are in Figure B.4.

533 6. Conclusions and Future Work

534 In this work a novel trading decision making workflow has been proposed
535 to generate effective buy or sell signals. In this proposal, the trading rules
536 are based on hybridizing technical analysis rules with the predictive power
537 of machine learning models.

538 From among all the machine learning techniques tested, LM and ANN
539 were the ones that performed best. The good performance of ANN is well
540 known in stock market prediction and, for that reason, has been extensively
541 used in previous work. The good performance of LM could suggest that for
542 smaller period of time the linear model is suitable for prediction purposes.

543 We have tested our proposal with TEMA and MACD trading strategies,
544 and we have proved the our strategy helped in obtaining superior results.
545 Hybridization not only has improved the profit but it also has decreased the
546 number of trades as well as the risk of losses.

547 It is also worth noticing that, for each algorithm used in the proposed
548 workflow, the optimal parameters depended on the index analyzed. Despite

549 the good results achieved, more research is necessary to enhance the under-
550 standing of the proposed workflow and trading rules.

551 As it has been shown in this work, the hybrid trading strategies achieve
552 good results. However the prediction horizon length h can be optimized.
553 Therefore, as future work, we intend to carry out the optimization of h
554 and validate it on new real data from other stock market indices, as well
555 as on foreign exchange market data. Another possible improvement of the
556 strategy is to incorporate trend information by addressing the problem as
557 a classification task. We also intend to address the exploration of more
558 technical analysis strategies and new trading rules. Finally, in order to gain
559 more insight about the predictive models, in future works more metrics will
560 be included in the study, such as precision, recall and F1-score [54] among
561 many others available.

562 **Appendix A. Results**

563 The tables shown in this section report, for each metric, the average
564 results together with its standard deviation. Such values are computed over
565 the prediction horizon h for each historical window w .

Table A.8: Results achieved by all the methods on IBEX averaged over the prediction horizon h for each historical window w .

w	Metric	LM	NN	RF	SVR
6	MAE	174.36 ± 49.57	179.08 ± 52.89	199.44 ± 51.36	174.05 ± 49.35
	RMSE	225.64 ± 63.71	230.46 ± 66.82	254.26 ± 63.98	226.11 ± 63.78
	sMAPE ¹	18.19 ± 5.19	18.69 ± 5.54	20.93 ± 5.43	18.15 ± 5.16
	MAPE ¹	18.17 ± 5.18	18.65 ± 5.52	20.89 ± 5.41	18.09 ± 5.13
12	MAE	174.10 ± 49.65	178.44 ± 52.81	196.79 ± 50.40	173.74 ± 49.28
	RMSE	225.24 ± 63.75	229.59 ± 66.62	249.40 ± 62.78	225.69 ± 63.57
	sMAPE ¹	18.17 ± 5.20	18.63 ± 5.53	20.64 ± 5.32	18.12 ± 5.15
	MAPE ¹	18.15 ± 5.19	18.60 ± 5.52	20.63 ± 5.32	18.06 ± 5.12
24	MAE	174.44 ± 49.74	178.52 ± 52.77	196.00 ± 49.68	173.48 ± 49.11
	RMSE	225.69 ± 63.65	229.64 ± 66.36	250.25 ± 62.06	225.17 ± 63.10
	sMAPE ¹	18.23 ± 5.22	18.65 ± 5.53	20.59 ± 5.25	18.10 ± 5.14
	MAPE ¹	18.21 ± 5.21	18.62 ± 5.52	20.58 ± 5.24	18.05 ± 5.11
48	MAE	173.95 ± 47.63	178.41 ± 50.85	200.48 ± 50.06	172.74 ± 47.14
	RMSE	224.69 ± 60.98	229.42 ± 64.22	254.41 ± 61.54	223.94 ± 60.68
	sMAPE ¹	18.21 ± 5.02	18.66 ± 5.35	21.10 ± 5.32	18.06 ± 4.95
	MAPE ¹	18.17 ± 5.00	18.61 ± 5.32	21.09 ± 5.30	17.98 ± 4.91
72	MAE	172.47 ± 47.21	177.78 ± 51.10	198.23 ± 48.34	172.00 ± 47.15
	RMSE	222.42 ± 60.56	227.95 ± 64.30	251.60 ± 59.91	222.57 ± 60.53
	sMAPE ¹	18.11 ± 5.00	18.65 ± 5.39	20.90 ± 5.15	18.03 ± 4.97
	MAPE ¹	18.07 ± 4.98	18.59 ± 5.37	20.86 ± 5.13	17.96 ± 4.94
96	MAE	172.91 ± 47.49	178.51 ± 51.35	194.93 ± 49.09	174.23 ± 48.28
	RMSE	223.38 ± 61.34	229.76 ± 65.41	247.73 ± 60.50	225.09 ± 62.20
	sMAPE ¹	18.18 ± 5.02	18.74 ± 5.41	20.57 ± 5.22	18.28 ± 5.08
	MAPE ¹	18.14 ± 5.01	18.69 ± 5.39	20.53 ± 5.19	18.21 ± 5.04
120	MAE	175.19 ± 49.46	179.48 ± 52.61	197.99 ± 51.07	176.78 ± 50.02
	RMSE	225.41 ± 62.66	230.98 ± 66.44	251.17 ± 62.63	227.48 ± 63.25
	sMAPE ¹	18.43 ± 5.23	18.86 ± 5.54	20.88 ± 5.40	18.56 ± 5.26
	MAPE ¹	18.40 ± 5.22	18.80 ± 5.52	20.84 ± 5.37	18.48 ± 5.22
168	MAE	180.96 ± 52.97	184.31 ± 55.41	210.29 ± 53.42	184.55 ± 54.35
	RMSE	231.11 ± 65.38	235.62 ± 68.39	265.79 ± 64.37	234.60 ± 66.61
	sMAPE ¹	19.06 ± 5.60	19.39 ± 5.85	22.21 ± 5.62	19.38 ± 5.71
	MAPE ¹	19.02 ± 5.59	19.33 ± 5.81	22.12 ± 5.57	19.29 ± 5.65
192	MAE	180.36 ± 51.95	184.36 ± 54.85	213.81 ± 57.38	184.78 ± 54.36
	RMSE	230.32 ± 64.65	235.52 ± 68.08	270.95 ± 68.08	234.71 ± 66.68
	sMAPE ¹	18.99 ± 5.49	19.38 ± 5.78	22.55 ± 6.02	19.42 ± 5.71
	MAPE ¹	18.92 ± 5.46	19.29 ± 5.73	22.40 ± 5.93	19.31 ± 5.66
216	MAE	176.65 ± 50.26	182.05 ± 54.28	210.87 ± 55.26	181.24 ± 53.10
	RMSE	226.94 ± 62.45	234.04 ± 67.30	267.32 ± 66.30	232.49 ± 65.97
	sMAPE ¹	18.58 ± 5.30	19.13 ± 5.71	22.24 ± 5.79	19.03 ± 5.58
	MAPE ¹	18.51 ± 5.27	19.03 ± 5.66	22.08 ± 5.70	18.93 ± 5.52
240	MAE	177.99 ± 52.21	183.45 ± 56.34	226.01 ± 56.01	183.31 ± 55.06
	RMSE	227.35 ± 64.05	234.64 ± 69.01	287.01 ± 67.86	233.75 ± 67.75
	sMAPE ¹	18.76 ± 5.53	19.32 ± 5.95	23.85 ± 5.87	19.29 ± 5.80
	MAPE ¹	18.71 ± 5.51	19.23 ± 5.91	23.65 ± 5.76	19.21 ± 5.75

¹ $\times 10^{-3}$.

Table A.9: Results achieved by all the methods on DAX averaged over the prediction horizon h for each historical window w .

w	Metric	LM	NN	RF	SVR
6	MAE	253.58 ± 82.98	253.82 ± 83.91	788.23 ± 36.07	252.58 ± 82.40
	RMSE	318.27 ± 98.99	321.03 ± 100.76	917.72 ± 31.98	318.43 ± 98.56
	sMAPE ¹	20.77 ± 6.78	20.77 ± 6.84	65.02 ± 3.07	20.68 ± 6.73
	MAPE ¹	20.77 ± 6.79	20.68 ± 6.80	67.90 ± 3.25	20.63 ± 6.72
12	MAE	253.56 ± 83.39	253.76 ± 84.23	784.00 ± 36.86	252.70 ± 82.71
	RMSE	318.40 ± 99.73	320.98 ± 101.40	913.47 ± 32.54	318.59 ± 99.18
	sMAPE ¹	20.77 ± 6.82	20.76 ± 6.87	64.66 ± 3.14	20.69 ± 6.75
	MAPE ¹	20.76 ± 6.83	20.68 ± 6.83	67.50 ± 3.32	20.64 ± 6.74
24	MAE	255.37 ± 83.51	260.38 ± 86.87	774.25 ± 35.18	253.77 ± 82.53
	RMSE	320.70 ± 100.31	331.16 ± 104.65	903.04 ± 30.91	319.77 ± 99.44
	sMAPE ¹	20.94 ± 6.83	21.27 ± 7.06	63.82 ± 3.00	20.79 ± 6.74
	MAPE ¹	20.94 ± 6.84	21.11 ± 6.98	66.59 ± 3.17	20.75 ± 6.73
48	MAE	257.37 ± 83.30	258.24 ± 84.79	739.87 ± 25.10	257.41 ± 83.48
	RMSE	325.21 ± 101.56	328.68 ± 104.12	866.68 ± 20.63	326.82 ± 102.16
	sMAPE ¹	21.10 ± 6.82	21.15 ± 6.92	60.88 ± 2.14	21.08 ± 6.82
	MAPE ¹	21.06 ± 6.80	21.04 ± 6.87	63.40 ± 2.24	20.99 ± 6.77
72	MAE	256.26 ± 81.82	257.37 ± 83.24	693.30 ± 19.57	257.38 ± 82.27
	RMSE	325.34 ± 100.65	329.07 ± 103.09	818.95 ± 15.05	329.07 ± 101.84
	sMAPE ¹	21.01 ± 6.69	21.08 ± 6.80	56.93 ± 1.68	21.08 ± 6.72
	MAPE ¹	20.95 ± 6.66	20.96 ± 6.73	59.15 ± 1.73	20.96 ± 6.65
96	MAE	254.73 ± 82.71	256.05 ± 83.87	660.71 ± 19.36	257.72 ± 83.00
	RMSE	324.30 ± 101.15	327.52 ± 103.14	785.09 ± 14.64	330.12 ± 102.27
	sMAPE ¹	20.89 ± 6.76	20.98 ± 6.85	54.18 ± 1.66	21.11 ± 6.77
	MAPE ¹	20.81 ± 6.73	20.86 ± 6.78	56.19 ± 1.70	20.96 ± 6.69
120	MAE	258.13 ± 84.36	259.22 ± 85.52	598.70 ± 21.27	260.72 ± 84.12
	RMSE	327.14 ± 102.52	330.78 ± 104.98	723.96 ± 15.20	331.86 ± 102.77
	sMAPE ¹	21.19 ± 6.91	21.25 ± 6.99	48.95 ± 1.82	21.37 ± 6.87
	MAPE ¹	21.13 ± 6.89	21.13 ± 6.92	50.63 ± 1.86	21.25 ± 6.81
168	MAE	259.88 ± 83.64	261.09 ± 85.15	526.24 ± 22.22	262.09 ± 83.84
	RMSE	332.81 ± 104.96	336.39 ± 107.47	650.74 ± 16.26	335.96 ± 104.70
	sMAPE ¹	21.31 ± 6.83	21.39 ± 6.94	42.91 ± 1.91	21.47 ± 6.83
	MAPE ¹	21.22 ± 6.78	21.25 ± 6.86	44.22 ± 1.93	21.31 ± 6.74
192	MAE	262.54 ± 85.69	265.74 ± 88.87	459.13 ± 25.10	264.54 ± 85.86
	RMSE	334.06 ± 105.36	341.63 ± 110.57	580.37 ± 19.47	338.50 ± 105.97
	sMAPE ¹	21.51 ± 6.99	21.74 ± 7.23	37.35 ± 2.15	21.66 ± 6.99
	MAPE ¹	21.41 ± 6.94	21.56 ± 7.12	38.32 ± 2.16	21.50 ± 6.90
216	MAE	263.62 ± 84.50	268.11 ± 88.78	433.33 ± 32.48	266.29 ± 85.06
	RMSE	333.45 ± 102.87	343.10 ± 109.36	551.45 ± 27.46	338.95 ± 103.90
	sMAPE ¹	21.62 ± 6.90	21.94 ± 7.22	35.24 ± 2.75	21.81 ± 6.93
	MAPE ¹	21.54 ± 6.88	21.75 ± 7.12	36.07 ± 2.78	21.66 ± 6.85
240	MAE	262.60 ± 83.28	266.17 ± 86.80	422.39 ± 37.95	265.03 ± 84.20
	RMSE	333.21 ± 102.40	341.50 ± 107.70	538.23 ± 32.97	339.21 ± 104.59
	sMAPE ¹	21.54 ± 6.80	21.78 ± 7.06	34.36 ± 3.21	21.70 ± 6.84
	MAPE ¹	21.49 ± 6.79	21.62 ± 6.97	35.12 ± 3.25	21.55 ± 6.75

¹ $\times 10^{-3}$.

Table A.10: Results achieved by all the methods on DJI averaged over the prediction horizon h for each historical window w .

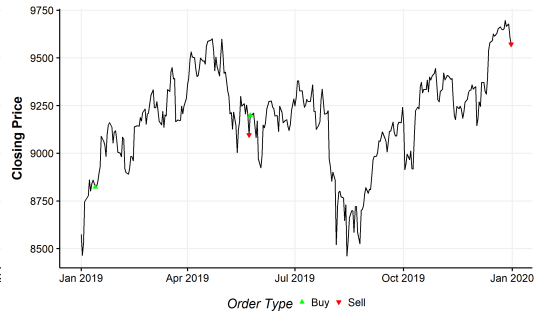
w	Metric	LM	NN	RF	SVR
6	MAE	483.86 ± 165.36	466.21 ± 154.70	4735.42 ± 7.68	488.15 ± 68.60
	RMSE	629.67 ± 190.43	625.06 ± 187.09	5060.00 ± 10.30	632.33 ± 91.88
	sMAPE ¹	19.36 ± 6.59	18.61 ± 6.14	207.42 ± 0.86	19.54 ± 6.73
	MAPE ¹	19.37 ± 6.62	18.56 ± 6.12	235.00 ± 1.15	19.56 ± 6.77
12	MAE	483.05 ± 164.29	466.93 ± 154.67	4680.76 ± 8.19	487.04 ± 66.35
	RMSE	628.65 ± 189.12	624.41 ± 186.13	5005.78 ± 10.99	631.06 ± 89.82
	sMAPE ¹	19.32 ± 6.55	18.64 ± 6.14	204.68 ± 0.88	19.49 ± 6.64
	MAPE ¹	19.33 ± 6.57	18.58 ± 6.12	231.55 ± 1.17	19.50 ± 6.67
24	MAE	482.09 ± 163.42	467.92 ± 154.92	4606.75 ± 6.39	486.23 ± 63.96
	RMSE	626.82 ± 187.64	623.31 ± 185.19	4930.32 ± 9.66	628.91 ± 87.72
	sMAPE ¹	19.27 ± 6.51	18.68 ± 6.15	200.95 ± 0.81	19.44 ± 6.54
	MAPE ¹	19.27 ± 6.53	18.61 ± 6.13	226.83 ± 1.07	19.45 ± 6.56
48	MAE	482.71 ± 162.10	469.09 ± 155.29	4654.86 ± 10.12	486.30 ± 60.86
	RMSE	628.25 ± 187.22	625.28 ± 185.52	4964.39 ± 12.78	630.84 ± 86.12
	sMAPE ¹	19.29 ± 6.46	18.72 ± 6.17	203.09 ± 1.01	19.44 ± 6.41
	MAPE ¹	19.28 ± 6.46	18.65 ± 6.14	229.36 ± 1.32	19.43 ± 6.42
72	MAE	482.15 ± 158.29	479.23 ± 157.60	4652.18 ± 11.89	484.41 ± 56.52
	RMSE	636.86 ± 187.59	636.76 ± 187.50	4951.54 ± 14.05	639.31 ± 84.80
	sMAPE ¹	19.22 ± 6.28	19.10 ± 6.25	202.76 ± 1.10	19.31 ± 6.21
	MAPE ¹	19.17 ± 6.26	19.03 ± 6.23	228.82 ± 1.42	19.27 ± 6.21
96	MAE	475.83 ± 154.16	474.28 ± 152.88	4633.87 ± 16.26	478.95 ± 51.32
	RMSE	631.39 ± 182.94	631.28 ± 182.74	4924.34 ± 17.84	634.76 ± 80.41
	sMAPE ¹	18.96 ± 6.12	18.90 ± 6.06	201.66 ± 1.31	19.09 ± 6.00
	MAPE ¹	18.90 ± 6.10	18.83 ± 6.04	227.34 ± 1.67	19.03 ± 5.99
120	MAE	479.78 ± 153.93	478.22 ± 153.35	4560.91 ± 16.41	488.52 ± 54.87
	RMSE	635.39 ± 183.19	635.38 ± 183.17	4845.72 ± 17.98	642.95 ± 83.80
	sMAPE ¹	19.11 ± 6.11	19.05 ± 6.08	197.93 ± 1.29	19.46 ± 6.14
	MAPE ¹	19.05 ± 6.09	18.98 ± 6.06	222.60 ± 1.64	19.40 ± 6.13
168	MAE	490.49 ± 155.99	474.29 ± 146.65	4584.66 ± 12.42	497.15 ± 53.16
	RMSE	644.57 ± 183.44	641.00 ± 180.86	4846.56 ± 14.56	651.35 ± 81.48
	sMAPE ¹	19.58 ± 6.22	18.90 ± 5.82	198.65 ± 1.11	19.82 ± 6.09
	MAPE ¹	19.56 ± 6.22	18.81 ± 5.79	223.24 ± 1.42	19.79 ± 6.08
192	MAE	496.02 ± 156.12	482.11 ± 149.13	4577.59 ± 16.49	503.18 ± 53.28
	RMSE	648.49 ± 183.05	645.82 ± 181.12	4829.97 ± 18.10	656.27 ± 81.69
	sMAPE ¹	19.78 ± 6.21	19.19 ± 5.91	198.11 ± 1.30	20.05 ± 6.09
	MAPE ¹	19.77 ± 6.22	19.11 ± 5.88	222.46 ± 1.65	20.02 ± 6.09
216	MAE	498.66 ± 157.25	485.03 ± 149.32	4544.00 ± 19.48	509.97 ± 57.85
	RMSE	649.19 ± 181.69	646.69 ± 179.51	4788.90 ± 20.16	661.68 ± 83.22
	sMAPE ¹	19.87 ± 6.26	19.30 ± 5.92	196.31 ± 1.44	20.30 ± 6.27
	MAPE ¹	19.86 ± 6.27	19.21 ± 5.88	220.13 ± 1.81	20.27 ± 6.28
240	MAE	509.90 ± 161.99	498.42 ± 156.53	4525.80 ± 23.90	518.01 ± 58.82
	RMSE	661.66 ± 188.15	660.06 ± 187.03	4761.43 ± 23.94	671.47 ± 85.66
	sMAPE ¹	20.31 ± 6.44	19.82 ± 6.21	195.22 ± 1.64	20.60 ± 6.31
	MAPE ¹	20.30 ± 6.45	19.74 ± 6.17	218.67 ± 2.04	20.58 ± 6.32

¹ × 10⁻³.

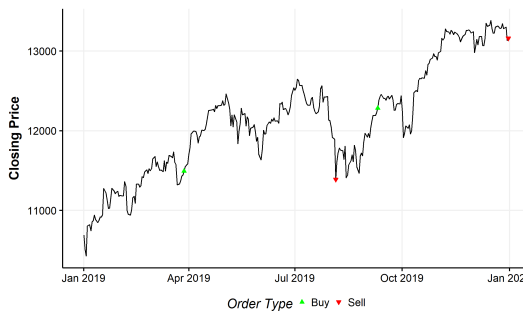
566 Appendix B. Trades



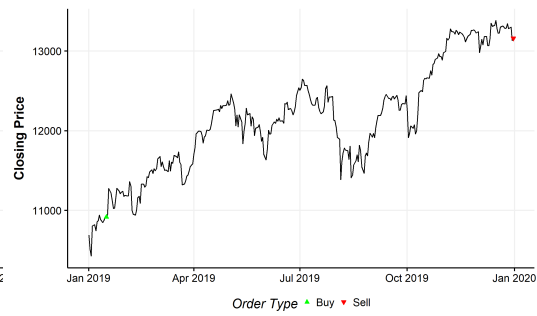
(a) Trades on 2019 IBEX data with TEMA.



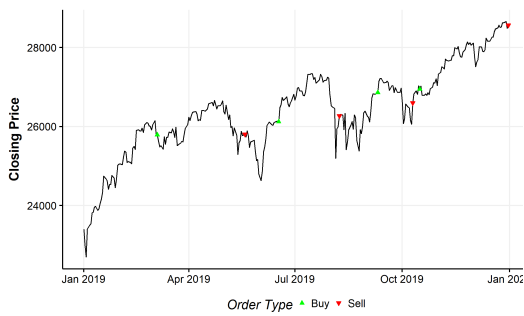
(b) Trades on 2019 IBEX data with hTEMA.



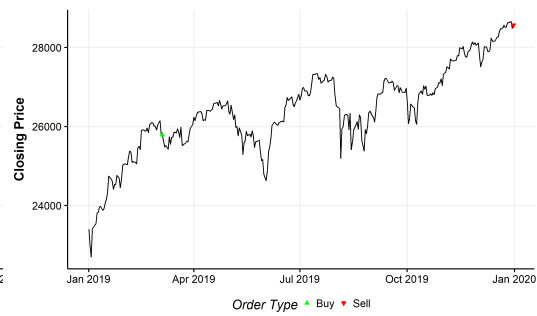
(c) Trades on 2019 DAX data with TEMA.



(d) Trades on 2019 DAX data with hTEMA.

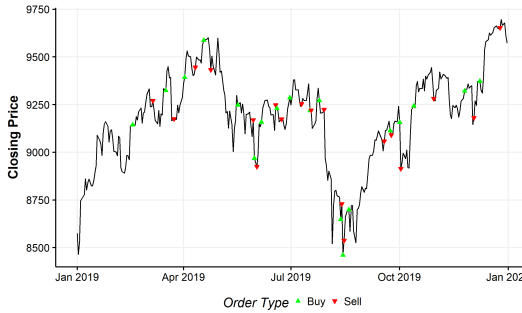


(e) Trades on 2019 DJI data with TEMA.

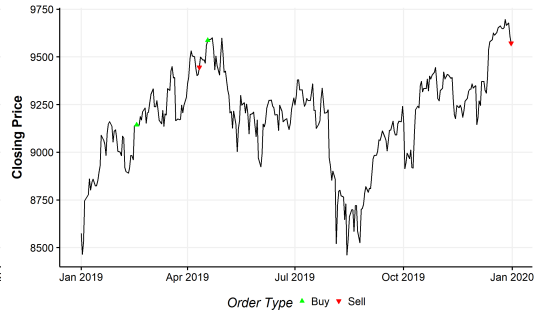


(f) Trades on 2019 DJI data with hTEMA.

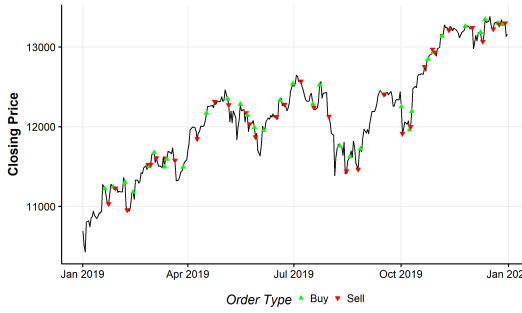
Figure B.3: Buy and sell signals found by TEMA and hTEMA trading strategies.



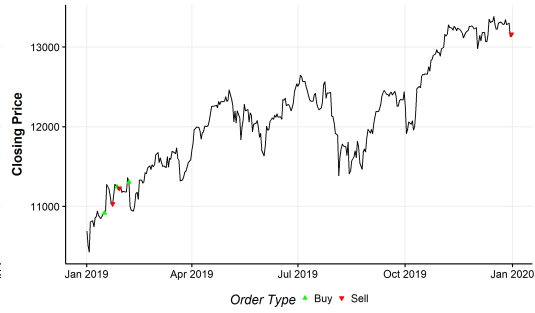
(a) Trades on 2019 IBEX data with MACD.



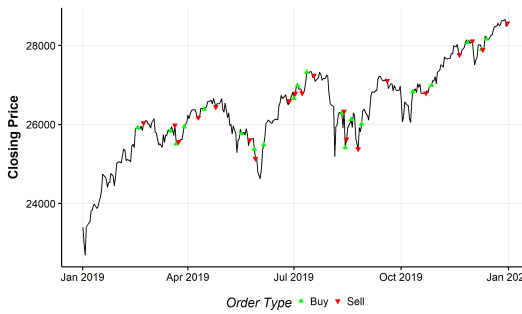
(b) Trades on 2019 IBEX data with hMACD.



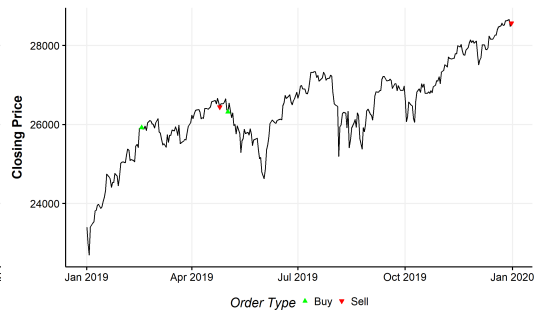
(c) Trades on 2019 DAX data with MACD.



(d) Trades on 2019 DAX data with hMACD.



(e) Trades on 2019 DJI data with MACD.



(f) Trades on 2019 DJI data with hMACD.

Figure B.4: Buy and sell signals found by MACD and hMACD trading strategies.

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